

**NP-3605**  
**B.Sc. (Com. Science)**  
**Examination, May-2024**

**Computer Oriented Numerical Techniques**  
**(BCS-401)**

*Time : Three Hours ] [Maximum Marks : 75*

**Section-A**

**Note :** Attempt **all** questions.

1. If  $f(x)=4\cos x-6x$ , find percentage error in  $f(x)$  for  $\Delta x=0.005$  and  $x=1$ . 3
2. Prove that  $(E^{1/2}+E^{-1/2})(1+\Delta)^{1/2}=2+\Delta$  3
3. Karl Pearson's coefficient of skewness of a distribution=0.32. S.D.=6.5, AM=29.6  
 From the above data find the mode and the median for the distribution. 3
4. Determine  $E(2X+5)$  3  
 The probability distribution of random

**P.T.O.**

variable X is  $P(x) = \frac{1}{2}, \frac{1}{6}, \frac{1}{3}, x=3, 1, -2$

5. Evaluate  $\int_1^2 \frac{dx}{1+x^2}$  taking  $h=0.2$ , using Trapezoidal Rule. 3

**Section-B**

**Note :** Attempt any **two** questions.

6. Using Lagrange's interpolation formula, find the value of  $y$  corresponding to  $x=3$  from the following table: 7.5

|      |     |     |     |     |
|------|-----|-----|-----|-----|
| x    | 0   | 1   | 2   | 4   |
| f(x) | 580 | 556 | 520 | 385 |

7. By the method of least squares, find the straight line that best fits the following data: 7.5

|   |    |    |    |    |    |
|---|----|----|----|----|----|
| x | 1  | 2  | 3  | 4  | 5  |
| y | 14 | 27 | 40 | 55 | 68 |

8. Using Poisson distribution, find the probability that the ace of spades will be drawn from a pack of well-shuffled cards atleast once in 104 consecutive trials. 7.5

**Section-C**

**Note :** Answer any **three** questions.

9. (a) Perform five iterations of the bisection method to obtain the smallest

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positive root of the equation

$$f(x) = x^3 - 5x + 1 = 0 \quad 7.5$$

(b) Find a solution of  $x^3 + x - 1 = 0$  by iteration method.

10. (a) Prove that  $\left(\frac{\Delta^2}{E}\right)e^x \cdot \frac{Ee^x}{\Delta^2 e^x} = e^x$  7.5  
the interval of differencing being  $h$ .

(b) From the following table, evaluate  $f(3.8)$  using Newton backward interpolation formula: 7.5

|        |      |      |      |      |      |
|--------|------|------|------|------|------|
| $x$    | 0    | 1    | 2    | 3    | 4    |
| $f(x)$ | 1.00 | 1.50 | 2.20 | 3.10 | 4.60 |

11. (a) Use Picard's method to approximate  $y$  when  $x=0.1$ , given that  $y=1$  when  $x=0$  and  $\frac{dy}{dx} = \frac{y-x}{y+x}$  7.5

(b) Estimate  $y(1)$  if  $2yy' = x^2$  and  $y(0) = 2$  using Runge-Kutta method of fourth order by taking  $h=0.5$ . Also compare the result with exact value. 7.5

12. (a) To test the effectiveness of inoculation against cholera, the following table was obtained. 7.5

|                |          |              |       |
|----------------|----------|--------------|-------|
|                | Attached | Not attached | Total |
| Inoculated     | 30       | 160          | 190   |
| Not Inoculated | 140      | 460          | 600   |
| Total          | 170      | 620          | 790   |

(The figures represent the number of persons) use  $\chi^2$ -test to defined or refute the statement. The inoculation prevents attack from cholera.

(b) A sample of 6 persons in an office revealed an average daily smoking of 10, 12, 8, 9, 16, 5 cigarettes. The average level of smoking in the whole office has to be estimated at 90% level of confidence.

$t=2.015$  for 5% degree of freedom. 7.5

13. (a) Apply Gauss forward formula to obtain  $f(x)$  at  $x=3.75$  from the table below: 7.5

|     |        |        |        |        |        |        |
|-----|--------|--------|--------|--------|--------|--------|
| $x$ | 2.5    | 3      | 3.5    | 4      | 4.5    | 5      |
| $y$ | 24.145 | 22.043 | 20.225 | 18.644 | 17.262 | 16.047 |

(b) Use Taylor series method to solve the equation

$$\frac{dy}{dx} = -xy, y(0) = 1 \quad 7.5$$